# Augmenting a ( $k-1$ )-Vetrex-Connected Multigraph to an - -Edge-Connected and $k$-Vetrex-Connected Multigraph 

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For two integers $k, l>0$ and an undirected multigraph $G=(V, E)$, we consider the problem of augmenting $G$ by the smallest number of new edges to obtain an l-edge-connected and $k$-vetrex-connected multigraph. In this paper we show that a ( $k-1$ )-vetrex-connected multigraph $G$ can be made $l$-edge-connected and $k$-vetrex-connected by adding at most max $\{l+1,2 k-4\}$ surplus edges over the optimum in $O\left(\min (k, \sqrt{n}) k n^{3}+n^{4}\right)$ time, where $n=|V|$.

